

Inference at \* 1 2 1 2 1 1 1  
of proof for Lemma less-fast-fib:

1.  $n : \mathbb{Z}$
  2.  $0 < n$
  3.  $\forall a, b : \mathbb{N}.$   
 $\{m : \mathbb{N} \mid$   
 $\forall k : \mathbb{N}.$   
 $(a = \text{fib}(k))$   
 $\Rightarrow ((k \leq 0) \Rightarrow (b = 0))$   
 $\Rightarrow ((0 < k) \Rightarrow (b = \text{fib}(k - 1)))$   
 $\Rightarrow (m = \text{fib}((n - 1) + k))\}$
  4.  $a : \mathbb{N}$
  5.  $b : \mathbb{N}$
  6.  $\forall b @ 0 : \mathbb{N}.$   
 $\{m : \mathbb{N} \mid$   
 $\forall k : \mathbb{N}.$   
 $(a + b = \text{fib}(k))$   
 $\Rightarrow ((k \leq 0) \Rightarrow (b @ 0 = 0))$   
 $\Rightarrow ((0 < k) \Rightarrow (b @ 0 = \text{fib}(k - 1)))$   
 $\Rightarrow (m = \text{fib}((n - 1) + k))\}$
  7.  $m : \mathbb{N}$
  8.  $\forall k : \mathbb{N}.$   
 $(a + b = \text{fib}(k))$   
 $\Rightarrow ((k \leq 0) \Rightarrow (a = 0))$   
 $\Rightarrow ((0 < k) \Rightarrow (a = \text{fib}(k - 1)))$   
 $\Rightarrow (m = \text{fib}((n - 1) + k))$
  9.  $k : \mathbb{N}$
  10.  $a = \text{fib}(k)$
  11.  $(0 < k) \Rightarrow (b = \text{fib}(k - 1))$
  12.  $k = 0$
  13.  $b = 0$
- $\vdash a + 0 = \text{fib}(0 + 1)$   
by (((if (first\_bool T:b) then HypSubst' else RevHypSubst') ( 10)( 0)) · )

CollapseTHEN (((if (first\_bool T:b) then HypSubst' else RevHypSubst') ( -2)( 0)) · )

1:

$$\vdash \text{fib}(0) + 0 = \text{fib}(0 + 1)$$